- 6 Let f be a twice-differentiable function such that f(2) = 5 and f(5) = 2. Let g be the function given by g(x) = f(f(x)).
- (a) Explain why there must be a value c for 2 < c < 5 such that f'(c) = -1.
- (b) Show that g'(2) = g'(5). Use this result to explain why there must be a value k for 2 < k < 5 such that g''(k) = 0.
- (c) Show that if f''(x) = 0 for all x, then the graph of g does not have a point of inflection.
- (d) Let h(x) = f(x) x. Explain why there must be a value r for 2 < r < 5 such that h(r) = 0.